

$$\begin{aligned} \textcircled{1} \quad G_1(y) &= G_{01} \cdot S_0(y) \cdot e^{-\lambda_1 \left(\frac{l}{2} - y\right)} \\ \textcircled{2} \quad G_2(y) &= G_{02} S_0(y) e^{-\lambda_2 \left(y + \frac{l}{2}\right)} \end{aligned} \quad \left. \vphantom{\begin{aligned} \textcircled{1} \quad G_1(y) &= G_{01} \cdot S_0(y) \cdot e^{-\lambda_1 \left(\frac{l}{2} - y\right)} \\ \textcircled{2} \quad G_2(y) &= G_{02} S_0(y) e^{-\lambda_2 \left(y + \frac{l}{2}\right)} \end{aligned}} \right\} \text{These are the signals observed by PRTs.}$$

First we need to match these gains in the center

$$\begin{aligned} \textcircled{3} \quad G_1(0) &= G_2(0) \\ G_{01} S_0(y) e^{-\lambda_1 \left(\frac{l}{2} - 0\right)} &= G_{02} S_0(y) e^{-\lambda_2 \left(0 + \frac{l}{2}\right)} \\ G_{01} e^{-\lambda_1 \frac{l}{2}} &= G_{02} e^{-\lambda_2 \frac{l}{2}} \end{aligned}$$

$$\boxed{\tilde{G}_{01} = \tilde{G}_{02}} \quad \text{This needs to be matched.}$$

$$G_1(y) = \tilde{G}_{01} \cdot S_0(y) e^{+\lambda_1 y}$$

$$G_2(y) = \tilde{G}_{02} S_0(y) e^{-\lambda_2 y} = \tilde{G}_{01} S_0(y) e^{-\lambda_2 y}$$

**AN:** 
$$\frac{G_1(y) + G_2(y)}{2} = \langle G(y) \rangle = \frac{1}{2} \tilde{G}_{01} S_0(y) \left( e^{+\lambda_1 y} + e^{-\lambda_2 y} \right) =$$

$$= \frac{1}{2} \tilde{G}_{01} S_0(y) \left( e^{+\lambda_1 y} + e^{-\lambda_2 y} \right) \quad \textcircled{5}$$

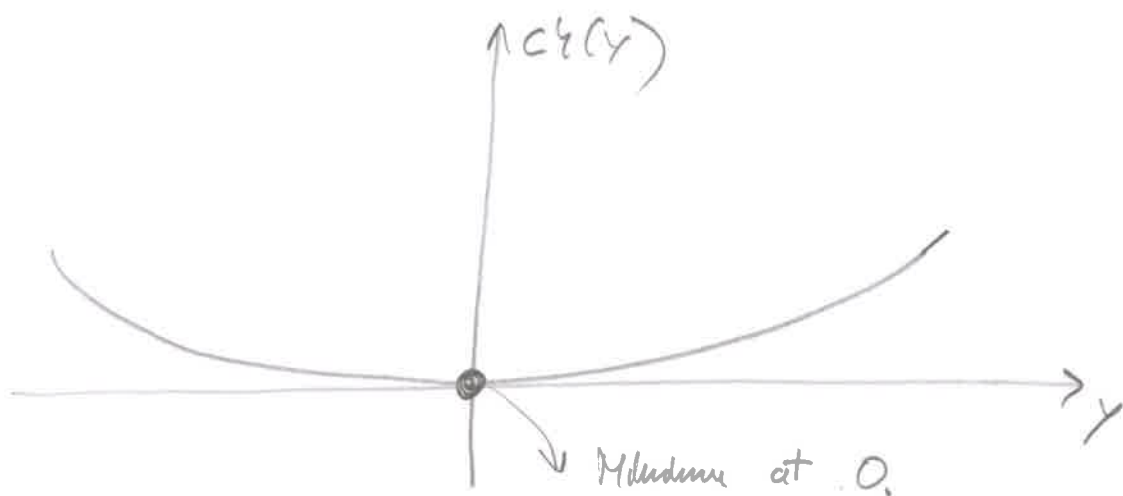
$$\delta G_1(y) := -(G_1(y) - G_1(0)) = \tilde{G}_{01} S_0(y) (-e^{\lambda_1 y} + e^{-\lambda_2 y}) =$$

$$= -2 \tilde{G}_{01} S_0(y) \left( \frac{e^{\lambda_1 y} - e^{-\lambda_2 y}}{2} \right) \quad (6)$$

①  $\lambda_1 = \lambda_2 :$

$$\langle G(y) \rangle = \tilde{G}_{01} S_0(y) \cdot \frac{e^{\lambda_1 y} + e^{-\lambda_1 y}}{2} =$$

$$= \tilde{G}_{01} S_0(y) \cdot \cosh(\lambda_1 y) \quad (7)$$



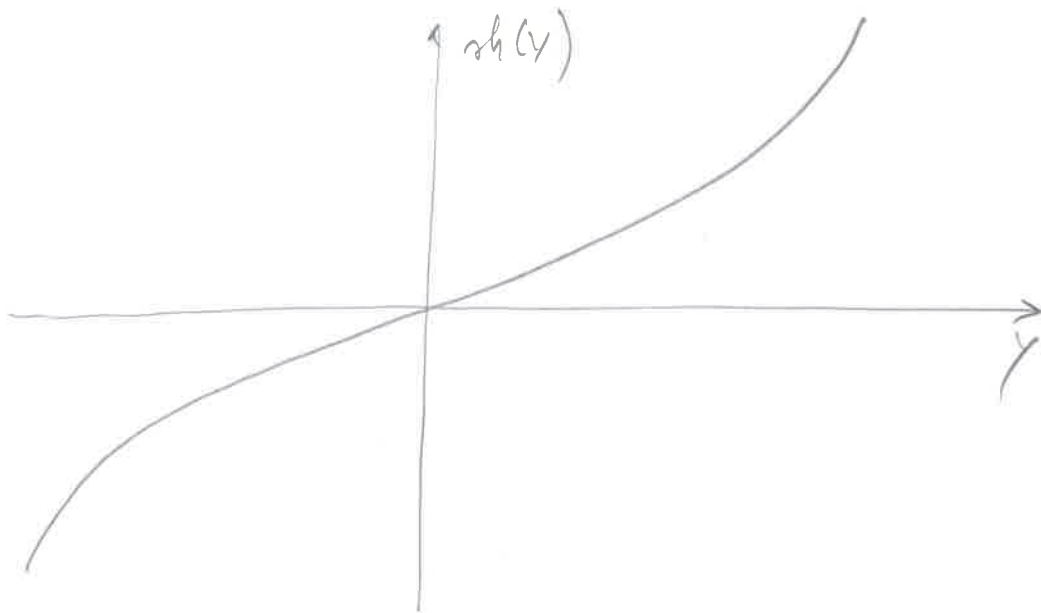
If we expand this into Taylor Series :

$$\langle G(y) \rangle = \tilde{G}_{01} S_0(y) \left[ 1 + \frac{y^2}{2} + \frac{y^4}{24} + \mathcal{O}(y^6) \right] \quad (8)$$

$$\delta G(\gamma) = 2 \tilde{G}_{01} S_0(\gamma) \frac{e^{\lambda_1 \gamma} - e^{-\lambda_1 \gamma}}{2} =$$

$$= 2 \tilde{G}_{01} S_0(\gamma) \cdot \text{sh}(\lambda_1 \gamma)$$

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If we expand thus:

$$\delta G(\gamma) = 2 \tilde{G}_{01} S_0(\gamma) \cdot \left[ x + \frac{x^3}{6} + \mathcal{O}(x^5) \right] \quad 10$$

## Geometric Mean:

$$\begin{aligned}\bar{q}(y) &= \sqrt{q_1(y) q_2(y)} = \tilde{q}_0 \cdot S_0(y) \cdot \sqrt{e^{\lambda_1 y} \cdot e^{-\lambda_2 y}} \\ &= \tilde{q}_0 S_0(y) e^{y \frac{(\lambda_1 - \lambda_2)}{2}}\end{aligned}\quad (11)$$

If  $\lambda_1 = \lambda_2$ :

$$\bar{q}(y) = \tilde{q}_0 S_0(y) \cdot 1$$

(12)

This is flat, independent of  $y$ !

If  $\lambda_1 \neq \lambda_2$  ( $\lambda_2 > \lambda_1$ )  $\Rightarrow$

